CSCI 420 Computer Graphics Lecture 14

#### Rasterization

Scan Conversion Antialiasing [Angel Ch. 6]

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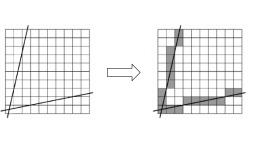
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## Rasterization (scan conversion)

- · Final step in pipeline: rasterization
- From screen coordinates (float) to pixels (int)
- · Writing pixels into frame buffer
- · Separate buffers:
  - depth (z-buffer),
  - display (frame buffer),
  - shadows (stencil buffer),
  - blending (accumulation buffer)

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## Rasterizing a line



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# Digital Differential Analyzer (DDA)

· Represent line as

$$y = mx + h$$

$$n = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$$

• Then, if  $\Delta x = 1$  pixel, we have  $\Delta y = m \Delta x = m$ 



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#### Digital Differential Analyzer

• Assume write\_pixel(int x, int y, int value)

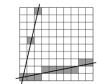
- Problems:
  - Requires floating point addition
  - Missing pixels with steep slopes: slope restriction needed



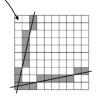
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## Digital Differential Analyzer (DDA)

- Assume 0 ≤ m ≤ 1
- Exploit symmetry
- Distinguish special cases

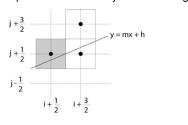


But still requires floating point additions!



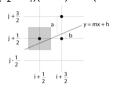
## Bresenham's Algorithm I

- · Eliminate floating point addition from DDA
- Assume again 0 ≤ m ≤ 1
- · Assume pixel centers halfway between integers



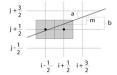
## Bresenham's Algorithm II

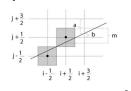
- Decision variable a b
  - If a b > 0 choose lower pixel
  - If  $a b \le 0$  choose higher pixel
- Goal: avoid explicit computation of a b
- Step 1: re-scale  $d = (x_2 x_1)(a b) = \Delta x(a b)$
- · d is always integer



Bresenham's Algorithm III

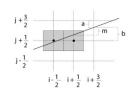
- Compute d at step k +1 from d at step k!
- Case: j did not change (d<sub>k</sub> > 0)
- a decreases by m, b increases by m
- (a b) decreases by 2m =  $2(\Delta y/\Delta x)$
- $\Delta x(a-b)$  decreases by  $2\Delta y$

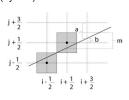




Bresenham's Algorithm IV

- Case: j did change (d<sub>k</sub> ≤ 0)
  - a decreases by m-1, b increases by m-1
  - (a b) decreases by 2m 2 = 2( $\Delta y/\Delta x 1$ )
  - $\Delta x(a-b)$  decreases by  $2(\Delta y \Delta x)$





Bresenham's Algorithm V

- So  $d_{k+1} = d_k 2\Delta y$  if  $d_k > 0$
- And  $d_{k+1} = d_k 2(\Delta y \Delta x)$  if  $d_k \le 0$
- Final (efficient) implementation:

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Bresenham's Algorithm VI

- Need different cases to handle m > 1
- · Highly efficient
- · Easy to implement in hardware and software
- · Widely used

#### Outline

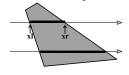
- · Scan Conversion for Lines
- Scan Conversion for Polygons
- · Antialiasing

#### Scan Conversion of Polygons

- · Multiple tasks:
  - Filling polygon (inside/outside)
  - Pixel shading (color interpolation)
  - Blending (accumulation, not just writing)
  - Depth values (z-buffer hidden-surface removal)
  - Texture coordinate interpolation (texture mapping)
- · Hardware efficiency is critical
- Many algorithms for filling (inside/outside)
- · Much fewer that handle all tasks well

### Filling Convex Polygons

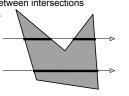
- · Find top and bottom vertices
- · List edges along left and right sides
- · For each scan line from bottom to top
  - Find left and right endpoints of span, xl and xr
  - Fill pixels between xl and xr
  - Can use Bresenham's algorithm to update xl and xr



## Concave Polygons: Odd-Even Test

- · Approach 1: odd-even test
- · For each scan line
  - Find all scan line/polygon intersections
  - Sort them left to right
  - Fill the interior spans between intersections

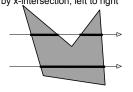
· Parity rule: inside after an odd number of crossings



#### Edge vs Scan Line Intersections

- · Brute force: calculate intersections explicitly
- Incremental method (Bresenham's algorithm)
- · Caching intersection information
  - Edge table with edges sorted by y<sub>min</sub>
  - Active edges, sorted by x-intersection, left to right

· Process image from smallest y<sub>min</sub> up



#### Concave Polygons: Tessellation

- · Approach 2: divide non-convex, non-flat, or non-simple polygons into triangles
- OpenGL specification
  - Need accept only simple, flat, convex polygons
  - Tessellate explicitly with tessellator objects
  - Implicitly if you are lucky
- · Most modern GPUs scan-convert only triangles

#### Flood Fill

- · Draw outline of polygon
- · Pick color seed
- · Color surrounding pixels and recurse
- Must be able to test boundary and duplication
- · More appropriate for drawing than rendering







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#### Outline

- · Scan Conversion for Lines
- · Scan Conversion for Polygons
- · Antialiasing

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## Aliasing

- · Artifacts created during scan conversion
- Inevitable (going from continuous to discrete)
- Aliasing (name from digital signal processing): we sample a continues image at grid points
- Effect
  - Jagged edges
  - Moire patterns



Moire pattern from sandlotscience.com

# More Aliasing



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## Antialiasing for Line Segments

· Use area averaging at boundary







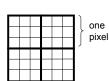


- (c) is aliased, magnified
- · (d) is antialiased, magnified

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## Antialiasing by Supersampling

- Mostly for off-line rendering (e.g., ray tracing)
- Render, say, 3x3 grid of mini-pixels
- Average results using a filter
- · Can be done adaptively
  - Stop if colors are similar
  - Subdivide at discontinuities



## Supersampling Example





- · Other improvements
  - Stochastic sampling: avoid sample position repetitions
  - Stratified sampling (jittering) : perturb a regular grid of samples

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## **Temporal Aliasing**

- Sampling rate is frame rate (30 Hz for video)
- · Example: spokes of wagon wheel in movies
- Solution: supersample in time and average
  - Fast-moving objects are blurred
  - Happens automatically with real hardware (photo and video cameras)
    - Exposure time is important (shutter speed)
  - Effect is called motion blur



Motion blur

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## Wagon Wheel Effect



Source: YouTube

# Motion Blur Example

Achieve by stochastic sampling in time

T. Porter, Pixar, 1984 16 samples / pixel / timestep



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## Summary

- Scan Conversion for Polygons
  - Basic scan line algorithm
  - Convex vs concave
  - Odd-even rules, tessellation
- · Antialiasing (spatial and temporal)
  - Area averaging
  - Supersampling
  - Stochastic sampling