

CSCI 420 Computer Graphics  
Lecture 8

## Hierarchical Models

Projections and Shadows  
Hierarchical Models  
[Angel Ch. 8]

Jernej Barbic  
University of Southern California

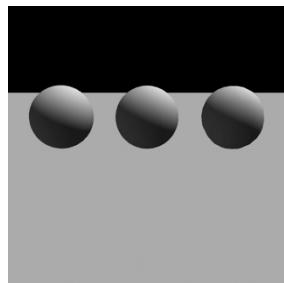
1

## Roadmap

- Last lecture: Viewing and projection
- Today:
  - Shadows via projections
  - Hierarchical models
- Next: Polygonal Meshes, Curves and Surfaces
- Goal: background for Assignment 2 (next week)

2

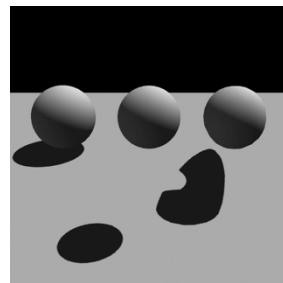
## Importance of shadows



Source: UNC

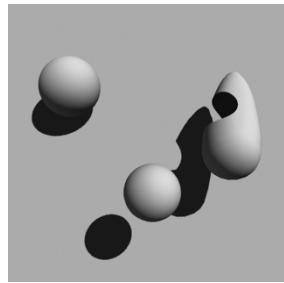
3

## Importance of shadows



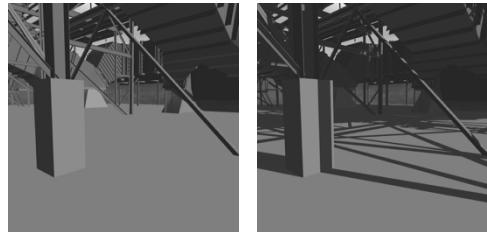
4

## Importance of shadows



5

## Importance of shadows



Without shadows

Source: UNC

With shadows

6

## Doom III

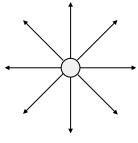


Source: Wikipedia

Reported to  
spend 50% of  
time rendering  
shadows!

7

## Light sources



point  
light source



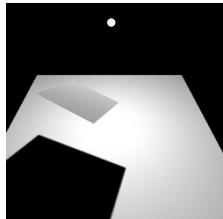
directional  
light source



area  
light source

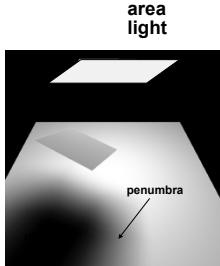
8

## Hard and soft shadows



Source: UNC

Hard shadow



Soft shadow

9

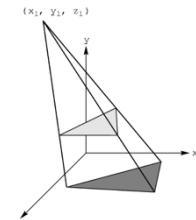
## Shadow Algorithms

- With visibility tests
  - Accurate yet expensive
  - Example: ray casting or ray tracing
  - Example: 2-pass z-buffer [Foley, Ch. 16.4.4] [RTR 6.12]
- Without visibility tests (“fake” shadows)
  - Approximate and inexpensive
  - Using a model-view matrix “trick”

10

## Shadows via Projection

- Assume light source at  $[x_l \ y_l \ z_l]^T$
- Assume shadow on plane  $y = 0$
- Viewing = shadow projection
  - Center of projection = light
  - Viewing plane = shadow plane
- View plane in front of object
- Shadow plane behind object



11

## Shadow Projection Strategy

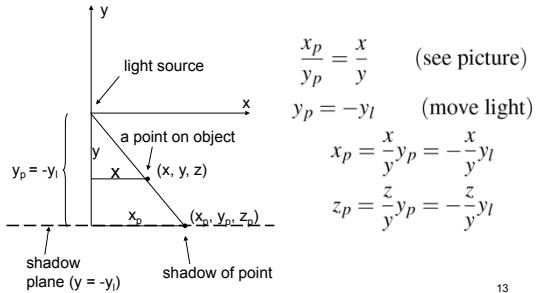
- Move light source to origin
- Apply appropriate projection matrix
- Move light source back
- Instance of general strategy: compose complex transformation from simpler ones!

$$T = \begin{bmatrix} 1 & 0 & 0 & -x_l \\ 0 & 1 & 0 & -y_l \\ 0 & 0 & 1 & -z_l \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

12

## Derive Equation

- Now, light source at origin

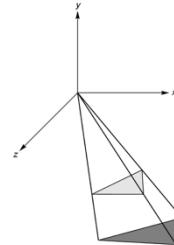


13

## Light Source at Origin

- After translation, solve

$$M \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = w \begin{bmatrix} -\frac{xy_l}{y} \\ -\frac{y_l}{y} \\ -\frac{zy_l}{y} \\ 1 \end{bmatrix}$$



14

## Shadow Projection Matrix

- Solution of previous equation

$$M = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & -\frac{1}{y_l} & 0 & 0 \end{bmatrix}$$

- Total shadow projection matrix

$$S = T^{-1}MT = \dots$$

15

## Implementation

- Recall column-major form

```
GLfloat m[16] =
{1.0, 0.0, 0.0, 0.0,
 0.0, 1.0, 0.0, -1.0 / yl,
 0.0, 0.0, 1.0, 0.0,
 0.0, 0.0, 0.0, 0.0};
```

- $yl$  is light source height
- Assume drawPolygon(); draws object

16

## Saving the ModelView Matrix State

- Assume  $x_l, y_l, z_l$  hold light coordinates
  - Core OpenGL code (compatibility code is similar)
- ```
openGLMatrix->MatrixMode(OpenGLMatrix::ModelView);
// here, set the model view matrix, in the usual way
// ...

drawPolygon(); // draw normally
openGLMatrix->PushMatrix(); // save current matrix
openGLMatrix->Translate(x_l, y_l, z_l); // translate back
openGLMatrix->MultMatrix(m); // project
openGLMatrix->Translate(-x_l, -y_l, -z_l); // move light to origin

float ms[16];
openGLMatrix->GetMatrix(ms); // read the shadow matrix
```

17

## Saving the ModelView Matrix State (cont.)

```
// upload the shadow matrix to the GPU
glUniformMatrix4fv(h_modelViewMatrix, 1, GL_FALSE, ms);

drawPolygon(); // draw polygon again for shadow

// restore original modelview matrix
openGLMatrix->PopMatrix();
openGLMatrix->GetMatrix(ms);
glUniformMatrix4fv(h_modelViewMatrix, 1, GL_FALSE, ms);

// continue rendering more objects, as usual ...
```

18

## The Matrix and Attribute Stacks

- Mechanism to save and restore state
  - `{OpenGLMatrix::, gl}PushMatrix();`
  - `{OpenGLMatrix::, gl}PopMatrix();`
- Apply to current matrix
- In compatibility profile, can also save current attribute values
  - Examples: color, lighting
  - `glPushAttrib(GLbitfield mask);`
  - `glPopAttrib();`
  - Mask determines which attributes are saved
  - This feature has been removed in the core profile

19

## Drawing on a Surface

- Shimmering (“z-buffer fighting”) when drawing shadow on surface
- Due to limited precision of depth buffer
- Solution: slightly displace either the surface or the shadow  
(`glPolygonOffset` in OpenGL)

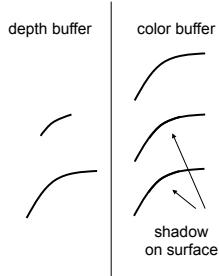


20

## Drawing on a Surface

Or use general technique

1. Set depth buffer to read-only, draw surface
2. Set depth buffer to read-write, draw shadow
3. Set color buffer to read-only, draw surface again
4. Set color buffer to read-write



21

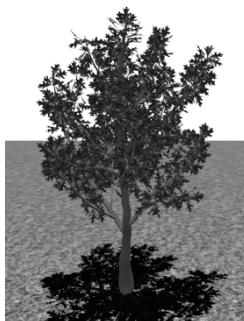
## Outline

- Projections and Shadows
- Hierarchical Models

22

## Hierarchical Models

- Many graphical objects are structured
- Exploit structure for
  - Efficient rendering
  - Example: tree leaves
  - Concise specification of model parameters
  - Example: joint angles
  - Physical realism
- Structure often naturally hierarchical



23

## Instance Transformation

- Often we need several instances of an object
  - Wheels of a car
  - Arms or legs of a figure
  - Chess pieces



24

## Instance Transformation

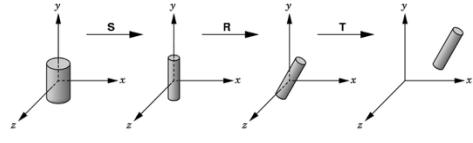
- Instances can be shared across space or time
- Write a function that renders the object in “standard” configuration
- Apply transformations to different instances
- Typical order: scaling, rotation, translation



25

## Sample Instance Transformation

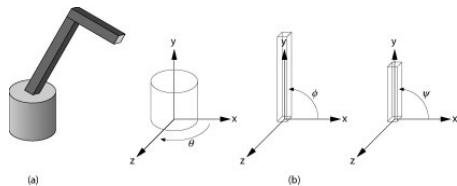
```
openGLMatrix->MatrixMode(OpenGLMatrix::ModelView);
openGLMatrix->LoadIdentity();
openGLMatrix->Translate(...);
openGLMatrix->Rotate(...);
openGLMatrix->Scale(...);
// ... upload modelview matrix to GPU, as usual ...
renderCylinder(...);
```



26

## Drawing a Compound Object

- Example: simple “robot arm”

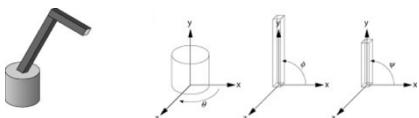


Base rotation  $\theta$ , arm angle  $\phi$ , joint angle  $\psi$

27

## Hierarchical Objects and Animation

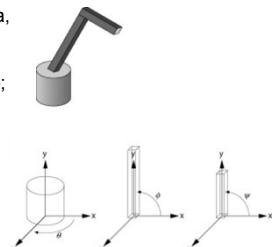
- Drawing functions are time-invariant and draw the object in a canonical position:  
drawBase(); drawLowerArm(); drawUpperArm();
- Can be easily stored in a VBO
- Change parameters of model with time



28

## Interleave Drawing & Transformation

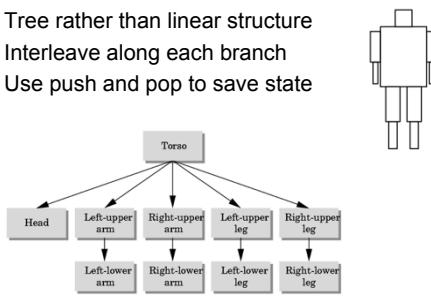
- $h1$  = height of base,  $h2$  = length of lower arm
  - This is pseudocode (must upload matrix to GPU)
- ```
void drawRobot(GLfloat theta, GLfloat phi, GLfloat psi)
{
    Rotate(theta, 0.0, 1.0, 0.0);
    drawBase();
    Translate(0.0, h1, 0.0);
    Rotate(phi, 0.0, 0.0, 1.0);
    drawLowerArm();
    Translate(0.0, h2, 0.0);
    Rotate(psi, 0.0, 0.0, 1.0);
    drawUpperArm();
}
```



29

## More Complex Objects

- Tree rather than linear structure
- Interleave along each branch
- Use push and pop to save state

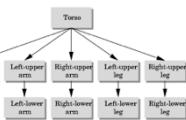


30

## Hierarchical Tree Traversal

- Order not necessarily fixed (breadth-first, depth-first, etc.)
- Example:

```
void drawFigure()
{
    PushMatrix(); // save
    drawTorso();
    Translate(...);
    Rotate(...);
    drawLeftUpperArm();
    Translate(...);
    Rotate(...);
    drawLeftLowerArm();
    PopMatrix();
    PushMatrix();
    ...
}
```



31

## Using Tree Data Structures

- Can make tree form explicit in data structure

```
typedef struct treenode
{
    GLfloat m[16];
    void (*render) ();
    struct treenode *sibling;
    struct treenode *child;
} treenode;
```

32

## Initializing Tree Data Structure

- Initializing transformation matrix for node

```
treenode torso, head, ...;
// in init function
LoadIdentity();
Rotate(...);
GetMatrix(torso.m);
```

- Initializing pointers

```
torso.render = drawTorso;
torso.sibling = NULL;
torso.child = &head;
```

33

## Generic Traversal: Recursion

```
void traverse (treenode *root)
{
    if (root == NULL)
        return;
    PushMatrix();
    MultMatrix(root->m);
    root->render();
    if (root->child != NULL)
        traverse(root->child);
    PopMatrix();
    if (root->sibling != NULL)
        traverse(root->sibling);
}
```

34

## Summary

- Projections and Shadows
- Hierarchical Models

35

## Notes

- Next lecture: polygonal meshes, curves and surfaces
- Assignment 1 is due in one week

36