CSCI 420 Computer Graphics Lecture 9

### Polygon Meshes and Implicit Surfaces

Polygon Meshes Implicit Surfaces Constructive Solid Geometry [Angel Ch. 10]

Jernej Barbic University of Southern California **Modeling Complex Shapes** 

 An equation for a sphere is possible, but how about an equation for a telephone, or a face?



- · Complexity is achieved using simple pieces
  - polygons, parametric surfaces, or implicit surfaces
- Goals
   Model anything with arbitrary precision (in principle)
  - Easy to build and modify
  - Efficient computations (for rendering, collisions, etc.)
     Easy to implement (a minor consideration...)

### What do we need from shapes in Computer Graphics?

- · Local control of shape for modeling
- · Ability to model what we need
- · Smoothness and continuity
- · Ability to evaluate derivatives
- · Ability to do collision detection
- Ease of rendering

No single technique solves all problems!

### **Shape Representations**

**Polygon Meshes Parametric Surfaces Implicit Surfaces** 

### **Polygon Meshes**

- · Any shape can be modeled out of polygons
  - if you use enough of them.
- Polygons with how many sides?
  - Can use triangles, quadrilaterals, pentagons, ... n-gons
  - Triangles are most common.
  - When > 3 sides are used, ambiguity about what to do when polygon nonplanar, or concave, or self-intersecting.
- Polygon meshes are built out of
  - vertices (points)
  - edges (line segments between vertices)
     faces (polygons bounded by edges)

edges

### **Normals** Triangle defines unique plane $\mathbf{n} = \frac{\mathbf{a} \times \mathbf{b}}{\|\mathbf{a} \times \mathbf{b}\|}$ depends on vertex orientation! clockwise order gives n' = -nVertex normals less well defined can average face normals works for smooth surfaces but not at sharp corners – think of a cube

### Where Meshes Come From

- · Specify manually
  - Write out all polygons
  - Write some code to generate them
  - Interactive editing: move vertices in space
- · Acquisition from real objects
  - Laser scanners, vision systems
  - Generate set of points on the surface
  - Need to convert to polygons









### **Data Structures for Polygon Meshes**

- Simplest (but dumb)
  - float triangle[n][3][3]; (each triangle stores 3 (x,y,z) points)
     redundant: each vertex stored multiple times
- · Vertex List, Face List

  - List of vertices, each vertex consists of (x,y,z) geometric (shape) info only

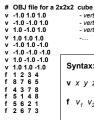
    List of triangles, each a triple of vertex id's (or pointers) topological (connectivity), adjacency) info only

    Fine for many purposes, but finding the faces adjacent to a vertex takes O(F) time for a model with F faces. Such queries are important for topological editing.
- · Fancier schemes:

Store more topological info so adjacency queries can be answered in O(1) time.

Winged-edge data structure – edge structures contain all topological info (pointers to adjacent vertices, edges, and faces).

### A File Format for Polygon Models: OBJ







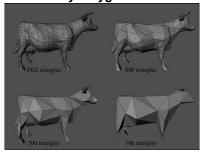
### Syntax:

**v** x y z - a vertex at (x,y,z)

- a face with

# anything - comment

**How Many Polygons to Use?** 



### Why Level of Detail?

- · Different models for near and far objects
- · Different models for rendering and collision detection
- Compression of data recorded from the real world

We need automatic algorithms for reducing the polygon count without

- losing key featuresgetting artifacts in the silhouettepopping

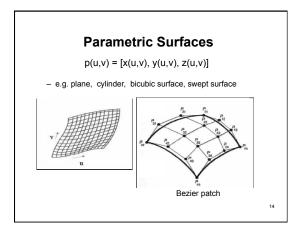
### **Problems with Triangular Meshes?**

- Need a lot of polygons to represent smooth shapes
- · Need a lot of polygons to represent detailed shapes
- · Hard to edit
- · Need to move individual vertices
- · Intersection test? Inside/outside test?

### **Shape Representations**

Polygon Meshes Parametric Surfaces Implicit Surfaces

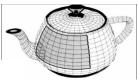
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### **Parametric Surfaces**

 $p(u,v) = [x(u,v),\,y(u,v),\,z(u,v)]$ 

- e.g. plane, cylinder, bicubic surface, swept surface



the Utah teapot

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### **Parametric Surfaces**

Why better than polygon meshes?

- Much more compact
- More convenient to control --- just edit control points
- Easy to construct from control points

What are the problems?

- Work well for smooth surfaces
- Must still split surfaces into discrete number of patches
- Rendering times are higher than for polygons
- Intersection test? Inside/outside test?

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### **Shape Representations**

Polygon Meshes Parametric Surfaces Implicit Surfaces

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### Two Ways to Define a Circle

Parametric Implicit

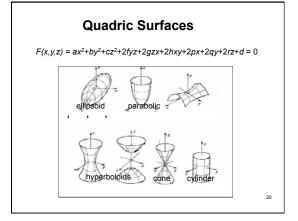
F>0
F=0

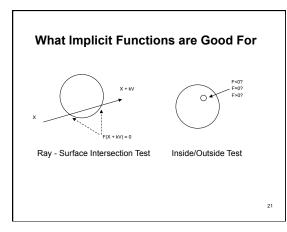
u

 $x = f(u) = r \cos(u)$  $y = g(u) = r \sin(u)$ 

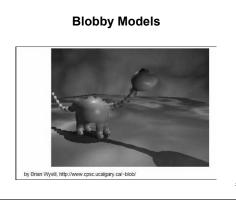
 $F(x,y) = x^2 + y^2 - r^2$ 

# Implicit Surfaces • well defined inside/outside • polygons and parametric surfaces do not have this information • Computing is hard: implicit functions for a cube? telephone? • Implicit surface: F(x,y,z) = 0• e.g. plane, sphere, cylinder, quadric, torus, blobby models sphere with radius r: $F(x,y,z) = x^2 + y^2 + z^2 - r^2 = 0$ - terrible for iterating over the surface - great for intersections, inside/outside test

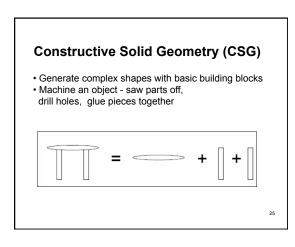


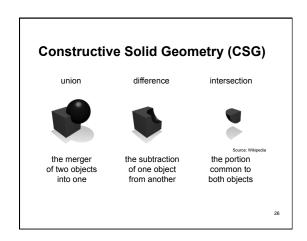


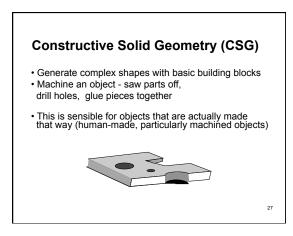
## Surfaces from Implicit Functions • Constant Value Surfaces are called (depending on whom you ask): - constant value surfaces - level sets - isosurfaces • Nice Feature: you can add them! (and other tricks) - this merges the shapes - When you use this with spherical exponential potentials, it's called Blobs, Metaballs, or Soft Objects. Great for modeling animals.

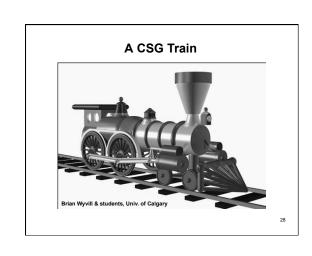


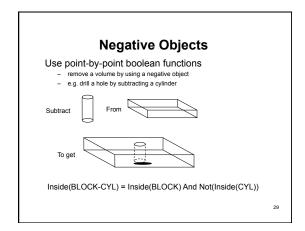
How to draw implicit surfaces?
 It's easy to ray trace implicit surfaces
 – because of that easy intersection test
 Volume Rendering can display them
 Convert to polygons: the Marching Cubes algorithm
 – Divide space into cubes
 – Evaluate implicit function at each cube vertex
 – Do root finding or linear interpolation along each edge
 – Polygonize on a cube-by-cube basis

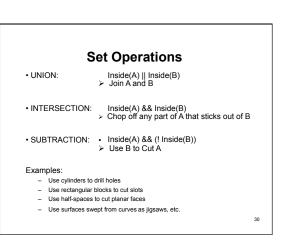












### **Implicit Functions for Booleans**

- Recall the implicit function for a solid: F(x,y,z)<0
- Boolean operations are replaced by arithmetic:

MAXMIN replaces AND (intersection) replaces OR (union)

- MINUS replaces NOT(unary subtraction)

- F(Intersect(A,B)) = MAX(F(A),F(B))
- F(Union(A,B)) = MIN(F(A),F(B))
- F(Subtract(A,B)) = MAX(F(A), -F(B))

F1<0

F1<0

F2<0

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F<sub>2</sub><0

### **CSG Trees** Set operations yield tree-based representation

### **Implicit Surfaces**

- Good for smoothly blending multiple components
- Clearly defined solid along with its boundary
- Intersection test and Inside/outside test are easy
- Need to polygonize to render --- expensive
- Interactive control is not easy
- Fitting to real world data is not easy
- Always smooth

### **Summary**

- Polygonal Meshes
- Parametric Surfaces
- Implicit Surfaces
- Constructive Solid Geometry