CSCI 420 Computer Graphics Lecture 14

### Rasterization

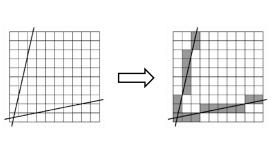
Scan Conversion Antialiasing [Angel Ch. 6]

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# Rasterization (scan conversion)

- Final step in pipeline: rasterization
- · From screen coordinates (float) to pixels (int)
- · Writing pixels into frame buffer
- Separate buffers:
  - depth (z-buffer),
  - display (frame buffer),
  - shadows (stencil buffer),
  - blending (accumulation buffer)

# Rasterizing a line



# Digital Differential Analyzer (DDA)

· Represent line as

$$y = mx + h$$
 where  $y = mx + h$ 

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$$

Then, if  $\Delta x = 1$  pixel, we have  $\Delta y = m \Delta x = m$ 

Assume 0 ≤ m ≤ 1

Exploit symmetry

cases

Distinguish special



# **Digital Differential Analyzer**

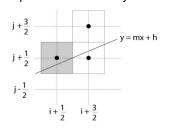
• Assume write\_pixel(int x, int y, int value)

- · Problems:
  - Requires floating point addition
  - Missing pixels with steep slopes: slope restriction needed

Digital Differential Analyzer (DDA) But still requires floating point additions!

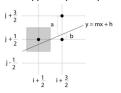
## Bresenham's Algorithm I

- · Eliminate floating point addition from DDA
- Assume again 0 ≤ m ≤ 1
- · Assume pixel centers halfway between integers



#### Bresenham's Algorithm II

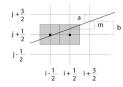
- Decision variable a b
  - If a b > 0 choose lower pixel
  - If  $a b \le 0$  choose higher pixel
- Goal: avoid explicit computation of a b
- Step 1: re-scale d =  $(x_2 x_1)(a b) = \Delta x(a b)$
- · d is always integer

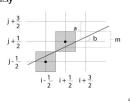


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### Bresenham's Algorithm III

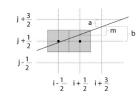
- Compute d at step k+1 from d at step k!
- Case: j did not change (d<sub>k</sub> > 0)
  - a decreases by m, b increases by m
  - (a b) decreases by 2m =  $2(\Delta y/\Delta x)$
  - ∆x(a-b) decreases by 2∆y

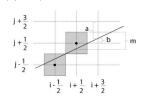




#### Bresenham's Algorithm IV

- Case: j did change (d<sub>k</sub> ≤ 0)
  - a decreases by m-1, b increases by m-1
  - -(a-b) decreases by  $2m-2=2(\Delta y/\Delta x-1)$
  - $\Delta x$ (a-b) decreases by 2( $\Delta y$   $\Delta x$ )





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# Bresenham's Algorithm V

- So  $d_{k+1} = d_k 2\Delta y$  if  $d_k > 0$
- And  $d_{k+1} = d_k 2(\Delta y \Delta x)$  if  $d_k \le 0$
- Final (efficient) implementation:

```
void draw_line(int x1, int y1, int x2, int y2) {
    int x, y = y0;
    int twice_dx = 2 * (x2 - x1), twice_dy = 2 * (y2 - y1);
    int twice_dy_minus_twice_dx = twice_dy - twice_dx;
    int d = twice_dx / 2 - twice_dy;

for (x = x1 ; x <= x2 ; x++) {
        write_pixel(x, y, color);
        if (d > 0) d -= twice_dy;
    else {y++; d -= twice_dy_minus_twice_dx ;}
}
```

## Bresenham's Algorithm VI

- Need different cases to handle m > 1
- · Highly efficient
- · Easy to implement in hardware and software
- · Widely used

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#### Outline

- · Scan Conversion for Lines
- · Scan Conversion for Polygons
- · Antialiasing

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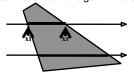
### Scan Conversion of Polygons

- · Multiple tasks:
  - Filling polygon (inside/outside)
  - Pixel shading (color interpolation)
  - Blending (accumulation, not just writing)
  - Depth values (z-buffer hidden-surface removal)
  - Texture coordinate interpolation (texture mapping)
- · Hardware efficiency is critical
- Many algorithms for filling (inside/outside)
- · Much fewer that handle all tasks well

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# Filling Convex Polygons

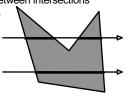
- · Find top and bottom vertices
- · List edges along left and right sides
- · For each scan line from bottom to top
  - Find left and right endpoints of span, xl and xr
  - Fill pixels between xl and xr
  - Can use Bresenham's algorithm to update xl and xr



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## Concave Polygons: Odd-Even Test

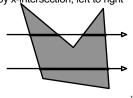
- · Approach 1: odd-even test
- · For each scan line
  - Find all scan line/polygon intersections
  - Sort them left to right
  - Fill the interior spans between intersections
- Parity rule: inside after an odd number of crossings



Edge vs Scan Line Intersections

- · Brute force: calculate intersections explicitly
- Incremental method (Bresenham's algorithm)
- · Caching intersection information
  - Edge table with edges sorted by  $y_{\text{min}}$
  - Active edges, sorted by x-intersection, left to right

 Process image from smallest y<sub>min</sub> up



#### Concave Polygons: Tessellation

- Approach 2: divide non-convex, non-flat, or non-simple polygons into triangles
- OpenGL specification
  - Need accept only simple, flat, convex polygons
  - Tessellate explicitly with tessellator objects
  - Implicitly if you are lucky
- Most modern GPUs scan-convert only triangles

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#### Flood Fill

- · Draw outline of polygon
- · Pick color seed
- · Color surrounding pixels and recurse
- · Must be able to test boundary and duplication
- · More appropriate for drawing than rendering







#### Outline

- · Scan Conversion for Lines
- · Scan Conversion for Polygons
- Antialiasing

#### Aliasing

- · Artifacts created during scan conversion
- · Inevitable (going from continuous to discrete)
- · Aliasing (name from digital signal processing): we sample a continues image at grid points
- · Effect
  - Jagged edges
  - Moire patterns



Moire pattern from sandlotscience.com

## More Aliasing



## **Antialiasing for Line Segments**

· Use area averaging at boundary





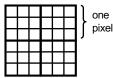




- (a) is aliased; (b) is antialiased
- (c) is aliased + magnified
- (d) is antialiased + magnified

# Antialiasing by Supersampling

- · Mostly for off-line rendering (e.g., ray tracing)
- · Render, say, 3x3 grid of mini-pixels
- · Average results using a filter
- Can be done adaptively
- Stop if colors are similar
- Subdivide at discontinuities



# Supersampling Example





- Other improvements
  - Stochastic sampling: avoid sample position repetitions
  - Stratified sampling (jittering) : perturb a regular grid of samples

# **Temporal Aliasing**

- Sampling rate is frame rate (30 Hz for video)
- Example: spokes of wagon wheel in movies
- Solution: supersample in time and average
  - Fast-moving objects are blurred
  - Happens automatically with real hardware (photo and video cameras)
    - Exposure time is important (shutter speed)
  - Effect is called motion blur



Motion blur

## Wagon Wheel Effect



Source: YouTube

# Motion Blur Example

Achieve by stochastic sampling in time

T. Porter, Pixar, 1984 16 samples / pixel / timestep



# Summary

- · Scan Conversion for Polygons
  - Basic scan line algorithm
  - Convex vs concave
  - Odd-even rules, tessellation
- · Antialiasing (spatial and temporal)
  - Area averaging
  - Supersampling
  - Stochastic sampling