CSCI 420 Computer Graphics Lecture 9

Polygon Meshes and Implicit Surfaces

Polygon Meshes Implicit Surfaces Constructive Solid Geometry [Angel Ch. 10]

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Modeling Complex Shapes

 An equation for a sphere is possible, but how about an equation for a telephone, or a face?



- · Complexity is achieved using simple pieces
 - polygons, parametric surfaces, or implicit surfaces
- Goals
 - Model anything with arbitrary precision (in principle)
 - Easy to build and modify
 - Efficient computations (for rendering, collisions, etc.)
 - Easy to implement (a minor consideration...)

What do we need from shapes in Computer Graphics?

- · Local control of shape for modeling
- · Ability to model what we need
- · Smoothness and continuity
- · Ability to evaluate derivatives
- · Ability to do collision detection
- · Ease of rendering

No single technique solves all problems!

Shape Representations

Polygon Meshes Parametric Surfaces Implicit Surfaces

Polygon Meshes

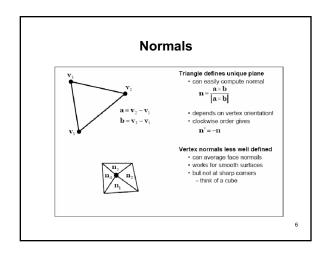
- · Any shape can be modeled out of polygons
 - if you use enough of them..
- Polygons with how many sides?
 - Can use triangles, quadrilaterals, pentagons, ... n-gons
 - Triangles are most common.
 - When > 3 sides are used, ambiguity about what to do when polygon nonplanar, or concave, or self-intersecting.
- · Polygon meshes are built out of

 - vertices (points)
 edges (line segments between vertices)
 - faces (polygons bounded by edges)









Where Meshes Come From

- · Specify manually
 - Write out all polygons
 - Write some code to generate them
 - Interactive editing: move vertices in space
- · Acquisition from real objects
 - Laser scanners, vision systems
 - Generate set of points on the surface
 - Need to convert to polygons









Data Structures for Polygon Meshes

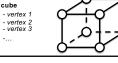
- Simplest (but dumb)
 - float triangle[n][3][3]; (each triangle stores 3 (x,y,z) points)
 - redundant: each vertex stored multiple times
- · Vertex List, Face List
- List of vertices, each vertex consists of (x,y,z) geometric (shape) info only
- List of triangles, each a triple of vertex id's (or pointers) topological (connectivity, adjacency) info only
 Fine for many purposes, but finding the faces adjacent to a vertex takes O(F) time for a model with F faces. Such queries are important for topological editing.
- · Fancier schemes:

Store more topological info so adjacency queries can be answered in $\mathrm{O}(1)$ time.

Winged-edge data structure – edge structures contain all topological info (pointers to adjacent vertices, edges, and faces).

A File Format for Polygon Models: OBJ

- # OBJ file for a 2x2x2 cube v -1.0 1.0 1.0 v -1.0 1.0 1.0 v -1.0 -1.0 1.0 v 1.0 -1.0 1.0 v 1.0 -1.0 1.0 v 1.0 1.0 1.0 v -1.0 1.0 -1.0 v -1.0 -1.0 -1.0 v 1.0 -1.0 -1.0 v 1.0 1.0 -1.0 f 1 2 3 4 f 8 7 6 5 f 4 3 7 8 f 5 1 4 8
 - vertex 2
 vertex 3

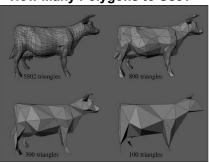


Syntax:

 \mathbf{v} \times \times \times \times - a vertex at (x,y,z)

> $\mathbf{f} \quad \mathbf{v}_1 \quad \mathbf{v}_2 \quad \dots \quad \mathbf{v}_n \quad \text{- a face with}$ vertices V₁, V₂, ... V_n

anything - comment **How Many Polygons to Use?**



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Why Level of Detail?

- · Different models for near and far objects
- · Different models for rendering and collision detection
- · Compression of data recorded from the real world

We need automatic algorithms for reducing the polygon count without

- · losing key features
- · getting artifacts in the silhouette
- popping

Problems with Triangular Meshes?

- · Need a lot of polygons to represent smooth shapes
- Need a lot of polygons to represent detailed shapes
- · Hard to edit
- · Need to move individual vertices
- · Intersection test? Inside/outside test?

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Shape Representations

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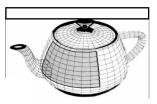
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Parametric Surfaces p(u,v) = [x(u,v), y(u,v), z(u,v)]- e.g. plane, cylinder, bicubic surface, swept surface $\frac{p_{a_1} - p_{a_2} - p_{a_3}}{p_{a_4} - p_{a_4}}$ Bezier patch

Parametric Surfaces

p(u,v) = [x(u,v), y(u,v), z(u,v)]

- e.g. plane, cylinder, bicubic surface, swept surface



the Utah teapot

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Parametric Surfaces

Why better than polygon meshes?

- Much more compact
- More convenient to control --- just edit control points
- Easy to construct from control points

What are the problems?

- Work well for smooth surfaces
- Must still split surfaces into discrete number of patches
- Rendering times are higher than for polygons
- Intersection test? Inside/outside test?

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Shape Representations

Polygon Meshes Parametric Surfaces Implicit Surfaces

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Two Ways to Define a Circle

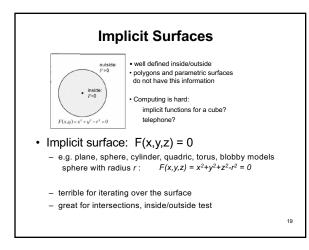


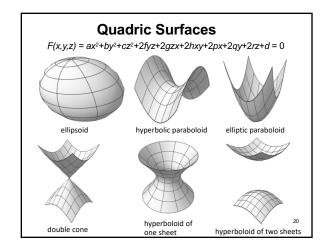
 $x = f(u) = r \cos(u)$ $y = g(u) = r \sin(u)$

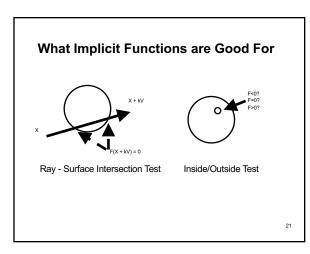


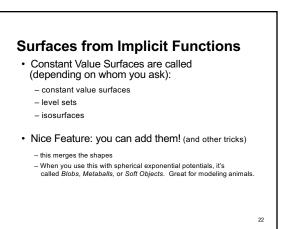
 $F(x,y) = x^2 + y^2 - r^2$

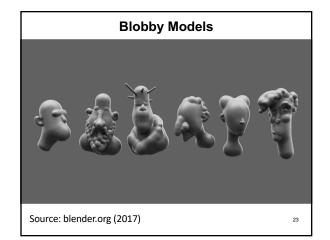
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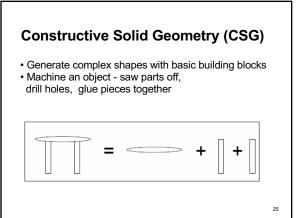


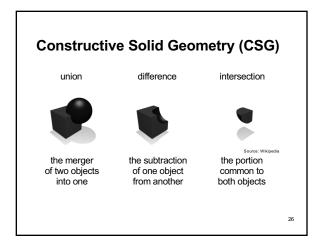






How to draw implicit surfaces? It's easy to ray trace implicit surfaces because of that easy intersection test Volume Rendering can display them Convert to polygons: the Marching Cubes algorithm Divide space into cubes Evaluate implicit function at each cube vertex Do root finding or linear interpolation along each edge Polygonize on a cube-by-cube basis





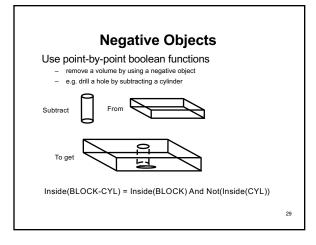


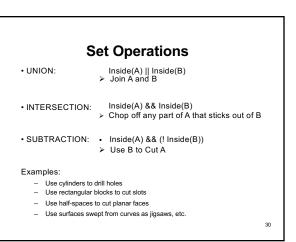
 This is sensible for objects that are actually made that way (human-made, particularly machined objects)



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Implicit Functions for Booleans

- Recall the implicit function for a solid: F(x,y,z)<0
- Boolean operations are replaced by arithmetic:

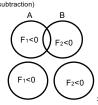
MAXMIN replaces AND (intersection) replaces OR (union)

- MINUS replaces NOT(unary subtraction)

• Thus

- F(Intersect(A,B)) = MAX(F(A),F(B))

- F(Union(A,B)) = MIN(F(A),F(B)) - F(Subtract(A,B)) = MAX(F(A), -F(B))



CSG Trees • Set operations yield tree-based representation

Implicit Surfaces

- Good for smoothly blending multiple components
- Clearly defined solid along with its boundary
- Intersection test and Inside/outside test are easy
- Need to polygonize to render --- expensive
- Interactive control is not easy
- Fitting to real world data is not easy
- Always smooth

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Summary

- Polygonal Meshes
- Parametric Surfaces
- Implicit Surfaces
- Constructive Solid Geometry