

CSCI 420 Computer Graphics
Lecture 11

Lighting and Shading

Light Sources
Phong Illumination Model
Normal Vectors
[Angel Ch. 5]

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Outline

- Global and Local Illumination
- Normal Vectors
- Light Sources
- Phong Illumination Model
- Polygonal Shading
- Example

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Global Illumination

- Ray tracing
- Radiosity
- Photon Mapping
- Follow light rays through a scene
- Accurate, but expensive (off-line)

Tobias R. Metoc

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Raytracing Example

Martin Moeck,
Siemens Lighting

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Radiosity Example

Restaurant Interior. Guillermo Leal, Evolucion Visual

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Local Illumination

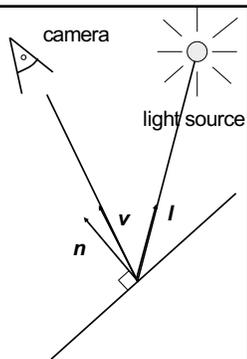
- Approximate model
- Local interaction between light, surface, viewer
- Phong model (this lecture): fast, supported in OpenGL
- GPU shaders
- Pixar Renderman (offline)

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Local Illumination

- Approximate model
- Local interaction between light, surface, viewer
- Color determined only based on surface normal, relative camera position and relative light position
- What effects does this ignore?



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Normal Vectors

- Must calculate and specify the normal vector
 - Even in OpenGL!
- Two examples: plane and sphere

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Normals of a Plane, Method I

- Method I: given by $ax + by + cz + d = 0$
- Let p_0 be a known point on the plane
- Let p be an arbitrary point on the plane
- Recall: $u \cdot v = 0$ if and only if u orthogonal to v
- $n \cdot (p - p_0) = n \cdot p - n \cdot p_0 = 0$
- Consequently $n_0 = [a \ b \ c]^T$
- Normalize to $n = n_0/|n_0|$

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Normals of a Plane, Method II

- Method II: plane given by p_0, p_1, p_2
- Points must not be collinear
- Recall: $u \times v$ orthogonal to u and v
- $n_0 = (p_1 - p_0) \times (p_2 - p_0)$
- Order of cross product determines orientation
- Normalize to $n = n_0/|n_0|$

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Normals of Sphere

- Implicit Equation $f(x, y, z) = x^2 + y^2 + z^2 - 1 = 0$
- Vector form: $f(p) = p \cdot p - 1 = 0$
- Normal given by gradient vector

$$n_0 = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \\ \frac{\partial f}{\partial z} \end{bmatrix} = \begin{bmatrix} 2x \\ 2y \\ 2z \end{bmatrix} = 2p$$

- Normalize $n_0/|n_0| = 2p/2 = p$

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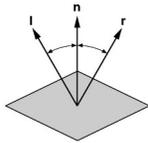
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Reflected Vector

- Perfect reflection: angle of incident equals angle of reflection
- Also: l , n , and r lie in the same plane
- Assume $|l| = |n| = 1$, guarantee $|r| = 1$



$$l \cdot n = \cos(\theta) = n \cdot r$$

$$r = \alpha l + \beta n$$

$$\text{Solution: } \alpha = -1 \text{ and } \beta = 2(l \cdot n)$$

$$r = 2(l \cdot n)n - l$$

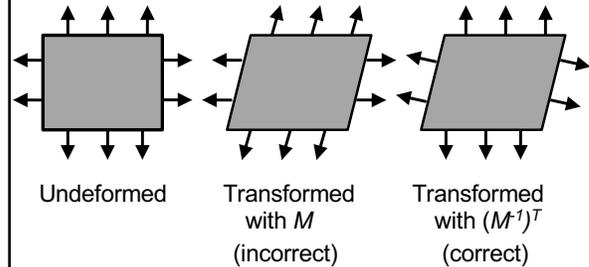
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Normals Transformed by Modelview Matrix

Modelview matrix M (shear in this example)

Only keep linear transform in M (discard any translation).

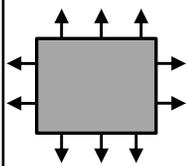


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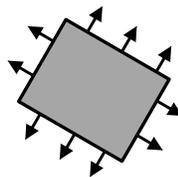
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Normals Transformed by Modelview Matrix

When M is rotation, $M = (M^{-1})^T$



Undeformed



Transformed with $M = (M^{-1})^T$
(correct)

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Normals Transformed by Modelview Matrix (proof of $(M^{-1})^T$ transform)

Point (x,y,z,w) is on a plane in 3D (homogeneous coordinates) if and only if

$$a x + b y + c z + d w = 0, \text{ or } [a \ b \ c \ d] [x \ y \ z \ w]^T = 0.$$

Now, let's transform the plane by M .

Point (x,y,z,w) is on the transformed plane if and only if

$M^{-1} [x \ y \ z \ w]^T$ is on the original plane:

$$[a \ b \ c \ d] M^{-1} [x \ y \ z \ w]^T = 0.$$

So, equation of transformed plane is

$$[a' \ b' \ c' \ d'] [x \ y \ z \ w]^T = 0, \text{ for}$$

$$[a' \ b' \ c' \ d']^T = (M^{-1})^T [a \ b \ c \ d]^T.$$

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Light Sources and Material Properties

- Appearance depends on
 - Light sources, their locations and properties
 - Material (surface) properties:



– Viewer position

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Types of Light Sources

- Ambient light: no identifiable source or direction
- Point source: given only by point
- Distant light: given only by direction
- Spotlight: from source in direction
 - Cut-off angle defines a cone of light
 - Attenuation function (brighter in center)



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Point Source

- Given by a point p_0
- Light emitted equally in all directions
- Intensity decreases with square of distance

$$I \propto \frac{1}{|p - p_0|^2}$$

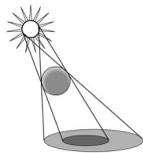
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Limitations of Point Sources

- Shading and shadows inaccurate
- Example: penumbra (partial “soft” shadow)
- Similar problems with highlights
- Compensate with attenuation

$$\frac{1}{a + bq + cq^2} \quad \begin{array}{l} q = \text{distance } |p - p_0| \\ a, b, c \text{ constants} \end{array}$$
- Softens lighting
- Better with ray tracing
- Better with radiosity

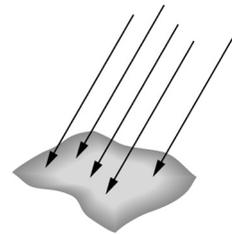


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Distant Light Source

- Given by a direction vector $[x \ y \ z]$

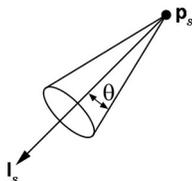


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Spotlight

- Light still emanates from point
- Cut-off by cone determined by angle θ



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Global Ambient Light

- Independent of light source
- Lights entire scene
- Computationally inexpensive
- Simply add $[G_R \ G_G \ G_B]$ to every pixel on every object
- Not very interesting on its own.
A cheap hack to make the scene brighter.

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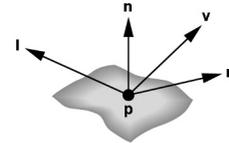
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Phong Illumination Model

- Calculate color for arbitrary point on surface
- Compromise between realism and efficiency
- Local computation (no visibility calculations)
- Basic inputs are material properties and \mathbf{l} , \mathbf{n} , \mathbf{v} :

\mathbf{l} = unit vector to light source
 \mathbf{n} = surface normal
 \mathbf{v} = unit vector to viewer
 \mathbf{r} = reflection of \mathbf{l} at \mathbf{p}
(determined by \mathbf{l} and \mathbf{n})



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Phong Illumination Overview

1. Start with global ambient light [G_R G_G G_B]
 2. Add contributions from each light source
 3. Clamp the final result to $[0, 1]$
- Calculate each color channel (R,G,B) **separately**
 - Light source contributions decomposed into
 - Ambient reflection
 - Diffuse reflection
 - Specular reflection
 - Based on ambient, diffuse, and specular lighting and material properties

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Ambient Reflection

$$I_a = k_a L_a$$

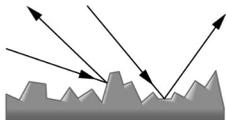
- Intensity of ambient light is uniform at every point
- Ambient reflection coefficient $k_a \geq 0$
- May be different for every surface and r,g,b
- Determines reflected fraction of ambient light
- L_a = ambient component of light source (can be set to different value for each light source)
- Note: L_a is not a physically meaningful quantity

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Diffuse Reflection

- Diffuse reflector scatters light
- Assume equally all direction
- Called Lambertian surface
- Diffuse reflection coefficient $k_d \geq 0$
- Angle of incoming light is important

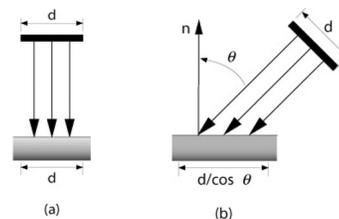


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Lambert's Law

Intensity depends on angle of incoming light.



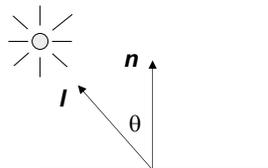
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Diffuse Light Intensity Depends On Angle Of Incoming Light

- Recall
 - I = unit vector to light
 - n = unit surface normal
 - θ = angle to normal
- $\cos \theta = I \cdot n$
- $I_d = k_d L_d (I \cdot n)$
- With attenuation:

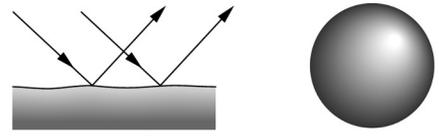
$$I_d = \frac{k_d L_d}{a + bq + cq^2} (I \cdot n)$$
 - q = distance to light source,
 - L_d = diffuse component of light



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Specular Reflection

- Specular reflection coefficient $k_s \geq 0$
- Shiny surfaces have high specular coefficient
- Used to model specular highlights
- Does not give the mirror effect (need other techniques)

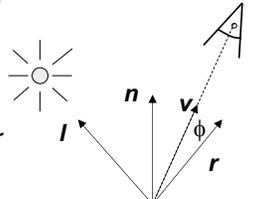


specular reflection specular highlights

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Specular Reflection

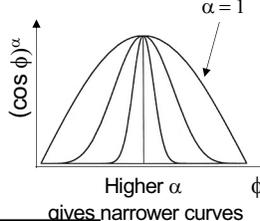
- Recall
 - v = unit vector to camera
 - r = unit reflected vector
 - ϕ = angle between v and r
- $\cos \phi = v \cdot r$
- $I_s = k_s L_s (\cos \phi)^\alpha$
- L_s is specular component of light
- α is shininess coefficient
- Can add distance term as well



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Shininess Coefficient

- $I_s = k_s L_s (\cos \phi)^\alpha$
- α is the shininess coefficient



low α high α

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Summary of Phong Model

- Light components for each color:
 - Ambient (L_a), diffuse (L_d), specular (L_s)
- Material coefficients for each color:
 - Ambient (k_a), diffuse (k_d), specular (k_s)
- Distance q for surface point from light source

$$I = \frac{1}{a + bq + cq^2} (k_d L_d (I \cdot n) + k_s L_s (r \cdot v)^\alpha) + k_a L_a$$

I = unit vector to light r = reflected about n
 n = surface normal v = vector to viewer

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BRDF

- Bidirectional Reflection Distribution Function
- Must measure for real materials
- Isotropic vs. anisotropic
- Mathematically complex
- Implement in a fragment shader



Lighting properties of a human face were captured and face re-rendered; Institute for Creative Technologies

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Outline

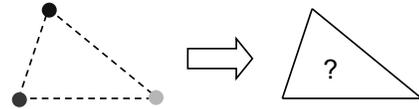
- Global and Local Illumination
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Polygonal Shading

- Now we know vertex colors
 - either via OpenGL lighting,
 - or by setting directly via `glColor3f` if lighting disabled
- How do we shade the interior of the triangle ?



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Polygonal Shading

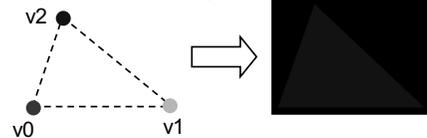
- Curved surfaces are approximated by polygons
- How do we shade?
 - Flat shading
 - Interpolative shading
 - Gouraud shading
 - Phong shading (different from Phong illumination!)

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Flat Shading

- Shading constant across polygon
- Core profile: Use interpolation qualifiers in the fragment shader
- Compatibility profile: Enable with `glShadeModel(GL_FLAT);`
- Color of last vertex determines interior color
- Only suitable for *very* small polygons

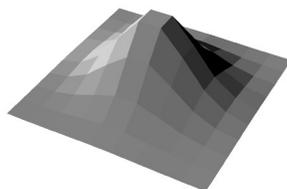


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Flat Shading Assessment

- Inexpensive to compute
- Appropriate for objects with flat faces
- Less pleasant for smooth surfaces

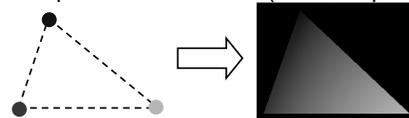


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Interpolative Shading

- Interpolate color in interior
- Computed during scan conversion (rasterization)
- Core profile: enabled by default
- Compatibility profile: enable with `glShadeModel(GL_SMOOTH);`
- Much better than flat shading
- More expensive to calculate (but not a problem)



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Gouraud Shading

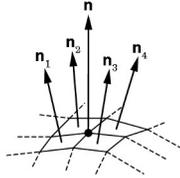
Invented by Henri Gouraud, Univ. of Utah, 1971

- Special case of interpolative shading
- How do we calculate vertex normals for a polygonal surface? Gouraud:
 1. average all adjacent face normals

$$n = \frac{n_1 + n_2 + n_3 + n_4}{|n_1 + n_2 + n_3 + n_4|}$$

2. use n for Phong lighting
3. interpolate vertex colors into the interior

- Requires knowledge about which faces share a vertex



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Data Structures for Gouraud Shading

- Sometimes vertex normals can be computed directly (e.g. height field with uniform mesh)
- More generally, need data structure for mesh
- Key: which polygons meet at each vertex

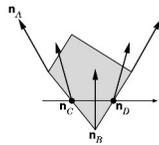
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Phong Shading (“per-pixel lighting”)

Invented by Bui Tuong Phong, Univ. of Utah, 1973

- *At each pixel* (as opposed to at each vertex) :
 1. Interpolate *normals* (rather than colors)
 2. Apply Phong lighting to the interpolated normal
- Significantly more expensive
- Done off-line or in GPU shaders (not supported in OpenGL directly)

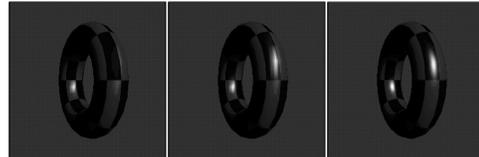


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Phong Shading Results

Michael Gold, Nvidia



Single light
Phong Lighting
Gouraud Shading

Two lights
Phong Lighting
Gouraud Shading

Two lights
Phong Lighting
Phong Shading

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Phong Shader: Vertex Program

```
#version 150
```

```
in vec3 position; } input vertex position and normal,
in vec3 normal;  } in world-space
```

```
out vec3 viewPosition; } vertex position and
out vec3 viewNormal;   } normal, in view-space } these will be
                                                                passed to
                                                                fragment
                                                                program
                                                                (interpolated by
                                                                hardware)
```

```
uniform mat4 modelViewMatrix; }
uniform mat4 normalMatrix;     } transformation matrices
uniform mat4 projectionMatrix; }
```

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Phong Shader: Vertex Program

```
void main()
{
    // view-space position of the vertex
    vec4 viewPosition4 = modelViewMatrix * vec4(position, 1.0f);
    viewPosition = viewPosition4.xyz;

    // final position in the normalized device coordinates space
    gl_Position = projectionMatrix * viewPosition4;
    // view-space normal
    viewNormal = normalize((normalMatrix*vec4(normal, 0.0f)).xyz);
}
```

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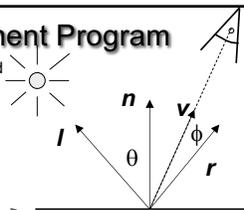
Phong Shader: Fragment Program

```
in vec3 viewPosition;
in vec3 viewNormal;

out vec4 c; // output color

uniform vec4 La; // light ambient
uniform vec4 Ld; // light diffuse
uniform vec4 Ls; // light specular
uniform vec3 viewLightDirection;

uniform vec4 ka; // mesh ambient
uniform vec4 kd; // mesh diffuse
uniform vec4 ks; // mesh specular
uniform float alpha; // shininess
```



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Phong Shader: Fragment Program

```
void main()
{
    // camera is at (0,0,0) after the modelview transformation
    vec3 eyedir = normalize(vec3(0, 0, 0) - viewPosition);
    // reflected light direction
    vec3 reflectDir = -reflect(viewLightDirection, viewNormal);
    // Phong lighting
    float d = max(dot(viewLightDirection, viewNormal), 0.0f);
    float s = max(dot(reflectDir, eyedir), 0.0f);
    // compute the final color
    c = ka * La + d * kd * Ld + pow(s, alpha) * ks * Ls;
}
```

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VBO and VAO setup

```
During initialization:
// Compute the unit normals (3 components per vertex).
// ...

// Put the normals coordinates into a VBO.
// 3 values per vertex, namely x,y,z components of the normal.
VBO * vboNormals = new VBO(numVertices, 3, normals,
    GL_STATIC_DRAW);

// Connect the shader variable "normal" to the VBO.
vao->ConnectPipelineProgramAndVBOAndShaderVariable(
    pipelineProgram, vboNormals, "normal");
```

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Upload the light direction vector to GPU

```
void display()
{
    glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT);
    openGLMatrix->SetMatrixMode(OpenGLMatrix::ModelView);
    openGLMatrix->LoadIdentity();
    openGLMatrix->LookAt(ex, ey, ez, fx, fy, fz, ux, uy, uz);

    float view[16];
    openGLMatrix->GetMatrix(view); // read the view matrix

    ...
}
```

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Upload the light direction vector to GPU

```
float lightDirection[3] = { 0, 1, 0 }; // the "Sun" at noon
float viewLightDirection[3]; // light direction in the view space
// the following line is pseudo-code:
viewLightDirection = (view * float4(lightDirection, 0.0)).xyz;

// upload viewLightDirection to the GPU
pipelineProgram->SetUniformVariable3fv("viewLightDirection",
    viewLightDirection);

// continue with model transformations
openGLMatrix->Translate(x, y, z);
...

renderBunny(); // render, via VAO
glutSwapBuffers();
```

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Upload the normal matrix to GPU

```
// in the display function:  
  
float n[16];  
matrix->SetMatrixMode(OpenGLMatrix::ModelView);  
matrix->GetNormalMatrix(n); // get normal matrix  
  
pipelineProgram->SetUniformVariableMatrix4fv(  
    "normalMatrix", GL_FALSE, m);
```

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