

CSCI 420 Computer Graphics  
Lecture 6

## Hierarchical Models

Projections and Shadows  
Hierarchical Models  
[Angel Ch 5.10, 10.1-10.6]

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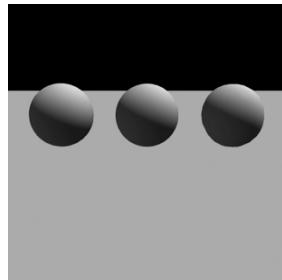
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## Roadmap

- Last lecture: Viewing and projection
- Today:
  - Shadows via projections
  - Hierarchical models
- Next: Polygonal Meshes, Curves and Surfaces
- Goal: background for Assignment 2 (next week)

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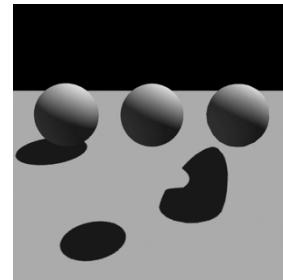
## Importance of shadows



Source: UNC

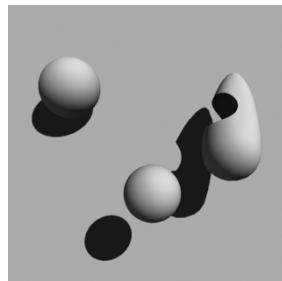
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## Importance of shadows



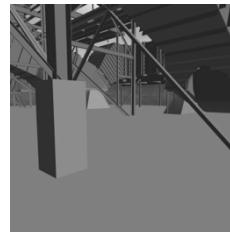
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## Importance of shadows

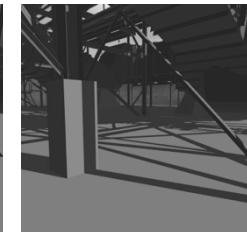


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## Importance of shadows



Without shadows



With shadows

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## Doom III

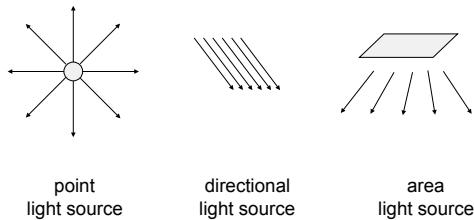


Source: Wikipedia

Reported to  
spend 50% of  
time rendering  
shadows!

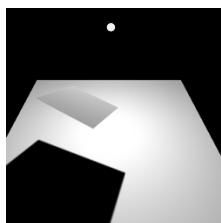
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## Light sources

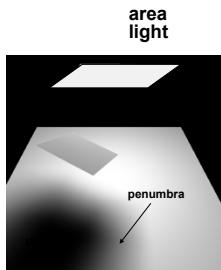


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## Hard and soft shadows



Source: UNC



Hard shadow

Soft shadow

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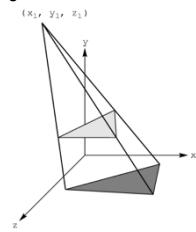
## Shadow Algorithms

- With visibility tests
  - Accurate yet expensive
  - Example: ray casting or ray tracing
  - Example: 2-pass z-buffer [Foley, Ch. 16.4.4] [RTR 6.12]
- Without visibility tests (“fake” shadows)
  - Approximate and inexpensive
  - Using a model-view matrix “trick”

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## Shadows via Projection

- Assume light source at  $[x_l \ y_l \ z_l]^T$
- Assume shadow on plane  $y = 0$
- Viewing = shadow projection
  - Center of projection = light
  - Viewing plane = shadow plane
- View plane in front of object
- Shadow plane behind object



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## Shadow Projection Strategy

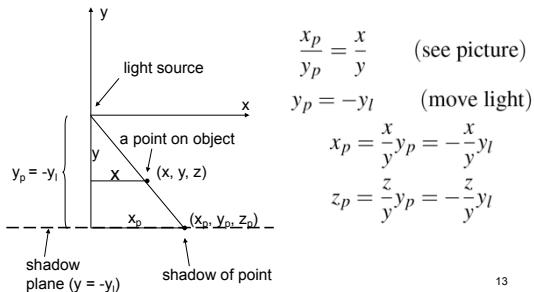
- Move light source to origin
- Apply appropriate projection matrix
- Move light source back
- Instance of general strategy: compose complex transformation from simpler ones!

$$T = \begin{bmatrix} 1 & 0 & 0 & -x_l \\ 0 & 1 & 0 & -y_l \\ 0 & 0 & 1 & -z_l \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

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## Derive Equation

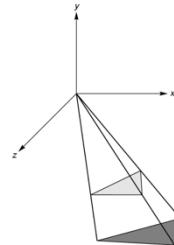
- Now, light source at origin



## Light Source at Origin

- After translation, solve

$$M \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = w \begin{bmatrix} -\frac{xy_l}{y} \\ -\frac{y_l}{y} \\ -\frac{zy_l}{y} \\ 1 \end{bmatrix}$$



- w can be chosen freely

- Use  $w = -y/y_l$

$$M \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \\ -\frac{y}{y_l} \end{bmatrix}$$

## Shadow Projection Matrix

- Solution of previous equation

$$M = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & -\frac{1}{y_l} & 0 & 0 \end{bmatrix}$$

- Total shadow projection matrix

$$S = T^{-1}MT = \dots$$

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## Implementation

- Recall column-major form

```
GLfloat m[16] =
{1.0, 0.0, 0.0, 0.0,
 0.0, 1.0, 0.0, -1.0 / yl,
 0.0, 0.0, 1.0, 0.0,
 0.0, 0.0, 0.0, 0.0};
```

- yl is light source height
- Assume drawPolygon(); draws object

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## Saving State

- Assume xl, yl, zl hold light coordinates

```
glMatrixMode(GL_MODELVIEW);
drawPolygon(); /* draw normally */

glPushMatrix(); /* save current matrix */
glTranslatef(xl, yl, zl); /* translate back */
glMultMatrixf(m); /* project */
glTranslatef(-xl, -yl, -zl); /* move light to origin */
drawPolygon(); /* draw polygon again for shadow */
glPopMatrix(); /* restore original transformation */
...
```

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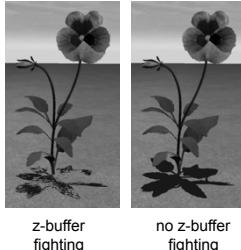
## The Matrix and Attribute Stacks

- Mechanism to save and restore state
  - glPushMatrix();
  - glPopMatrix();
- Apply to current matrix
- Can also save current attribute values
  - Examples: color, lighting
  - glPushAttrib(GLbitfield mask);
  - glPopAttrib();
  - Mask determines which attributes are saved

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## Drawing on a Surface

- Shimmering (“z-buffer fighting”) when drawing shadow on surface
- Due to limited precision of depth buffer
- Solution: slightly displace either the surface or the shadow  
(`glPolygonOffset` in OpenGL)

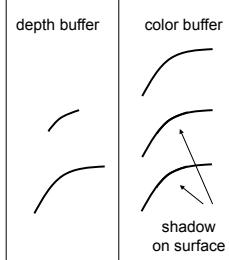


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## Drawing on a Surface

Or use general technique

1. Set depth buffer to read-only, draw surface
2. Set depth buffer to read-write, draw shadow
3. Set color buffer to read-only, draw surface again
4. Set color buffer to read-write



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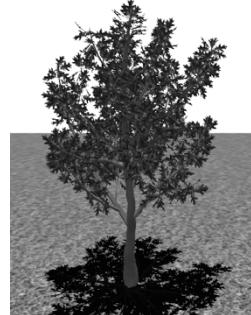
## Outline

- Projections and Shadows
- Hierarchical Models

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## Hierarchical Models

- Many graphical objects are structured
- Exploit structure for
  - Efficient rendering
  - Example: tree leaves
  - Concise specification of model parameters
  - Example: joint angles
  - Physical realism
- Structure often naturally hierarchical



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## Instance Transformation

- Often we need several instances of an object
  - Wheels of a car
  - Arms or legs of a figure
  - Chess pieces



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## Instance Transformation

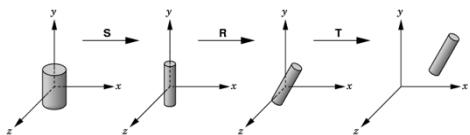
- Instances can be shared across space or time
- Write a function that renders the object in “standard” configuration
- Apply transformations to different instances
- Typical order: scaling, rotation, translation



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## Sample Instance Transformation

```
glMatrixMode(GL_MODELVIEW);
glLoadIdentity();
glTranslatef(...);
glRotatef(...);
glScalef(...);
gluCylinder(...);
```



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## Display Lists

- Sharing display commands
  - Display lists are stored on the GPU
  - May contain drawing commands and transfsns.
  - Initialization:
- ```
GLuint torus = glGenLists(1);
glNewList(torus, GL_COMPILE);
Torus(8, 25);
glEndList();
```
- Use: glCallList(torus);
  - Can share both within each frame, and across different frames in time
  - Can be hierarchical: a display list may call another

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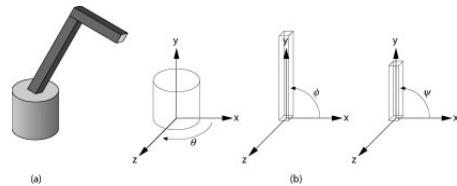
## Display Lists Caveats

- Store only results of expressions, not the expressions themselves
- Display lists cannot be changed or updated
- Effect of executing display list depends on current transformations and attributes
- Some implementation-dependent nesting limit
- They are deprecated:
  - for complex usage, use Vertex Buffer Object OpenGL extension instead

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## Drawing a Compound Object

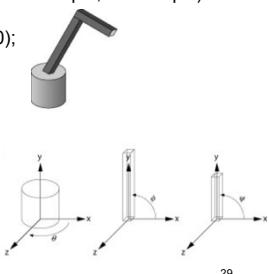
- Example: simple “robot arm”

Base rotation  $\theta$ , arm angle  $\phi$ , joint angle  $\psi$ 

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## Interleave Drawing & Transformation

```
h1 = height of base, h2 = length of lower arm
void drawRobot(GLfloat theta, GLfloat phi, GLfloat psi)
{
    glRotatef(theta, 0.0, 1.0, 0.0);
    drawBase();
    glTranslatef(0.0, h1, 0.0);
    glRotatef(phi, 0.0, 0.0, 1.0);
    drawLowerArm();
    glTranslatef(0.0, h2, 0.0);
    glRotatef(psi, 0.0, 0.0, 1.0);
    drawUpperArm();
}
```



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## Assessment of Interleaving

- Compact
- Correct “by construction”
- Efficient
- Inefficient alternative:
 

```
glPushMatrix();           glPushMatrix();           ...etc...
glRotatef(theta, ...);   glRotatef(theta, ...);
drawBase();               glTranslatef(...);
glPopMatrix();           glRotatef(phi, ...);
                        drawLowerArm();
                        glPopMatrix();
```
- Count number of transformations

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## Hierarchical Objects and Animation

- Drawing functions are time-invariant  
drawBase(); drawLowerArm(); drawUpperArm();
- Can be easily stored in display list
- Change parameters of model with time
- Redraw when idle callback is invoked

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## A Bug to Watch

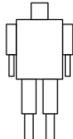
```
GLfloat theta = 0.0; ...; /* update in idle callback */
GLfloat phi = 0.0; ...; /* update in idle callback */
GLuint arm = glGenLists(1);
/* in init function */
glNewList(arm, GL_COMPILE);
glRotatef(theta, 0.0, 1.0, 0.0);
drawBase();

...
drawUpperArm();           What is wrong?
glEndList();
/* in display callback */
glCallList(arm);
```

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## More Complex Objects

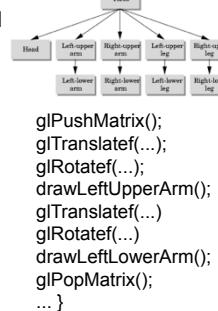
- Tree rather than linear structure
- Interleave along each branch
- Use push and pop to save state



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## Hierarchical Tree Traversal

- Order not necessarily fixed
- Example:



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## Using Tree Data Structures

- Can make tree form explicit in data structure
- ```
typedef struct treenode
{
    GLfloat m[16];
    void (*f) ();
    struct treenode *sibling;
    struct treenode *child;
} treenode;
```

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## Initializing Tree Data Structure

- Initializing transformation matrix for node
 

```
treenode torso, head, ...;
/* in init function */
glLoadIdentity();
glRotatef(...);
glGetFloatv(GL_MODELVIEW_MATRIX, torso.m);
```
- Initializing pointers
 

```
torso.f = drawTorso;
torso.sibling = NULL;
torso.child = &head;
```

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## Generic Traversal

- Recursive definition

```
void traverse (treenode *root)
{
    if (root == NULL) return;
    glPushMatrix();
    glMultMatrixf(root->m);
    root->f();
    if (root->child != NULL) traverse(root->child);
    glPopMatrix();
    if (root->sibling != NULL) traverse(root->sibling);
}
```
- C is really not the right language for this

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## Summary

- Projections and Shadows
- Hierarchical Models

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## Notes

- Wednesday – polygonal meshes, curves and surfaces
- Assignment 1 is due in one week

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